

EXERCISE 1

, lesson 6, slides 6 and 7

$S = 15$

$n = 145$

$\bar{x} = 100$

LC 95% $\rightarrow z = 1.96$

a. $E = z_{\alpha/2} \cdot \sigma_{\bar{x}} = 1.96 \cdot 1.25 = 2.45$

$\sigma_{\bar{x}} = \frac{S}{\sqrt{n-1}} = \frac{15}{\sqrt{145-1}} = \frac{15}{12} = 1.25$

↑
lesson 6, slide 7

, lesson 6, slide 7

b. $|\bar{x} \pm E| = 100 \pm 2.45 < \begin{matrix} 102.45 \\ 97.55 \end{matrix}$

EXERCISE 2

$\pi = 0.33$

$p = \frac{90}{250} = 0.36$

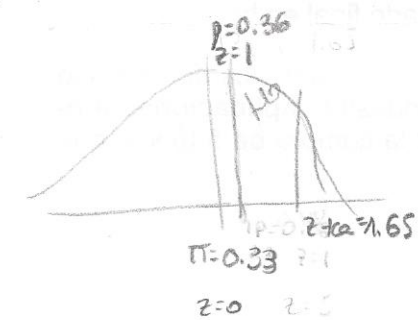
$H_0: \pi = p$

$z = \frac{p - \pi}{\sigma_p} = \frac{0.36 - 0.33}{0.03} = \frac{0.03}{0.03} = 1$

$\alpha = 0.1 \rightarrow z = 1.65$

$\sigma_p = \sqrt{\frac{\pi(1-\pi)}{n}} = \sqrt{\frac{0.33(1-0.33)}{250}} = 0.03$

$= \sqrt{\frac{0.33 \cdot 0.67}{250}} = \sqrt{\frac{0.2211}{250}} = \sqrt{0.0008844} = 0.03$



Conclusion with $z: 1$

$z_{emp} = 1 < z_{\alpha} = 1.65 - H_0$

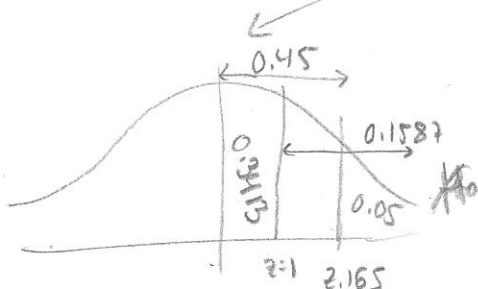
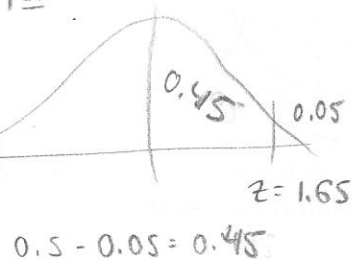
The planned percentage (33%) was statistically maintained

Conclusion with sig:)

$0.1587 \cdot 2 = 0.3174$

$p > \alpha - H_0$
 $0.3174 > 0.1$

• From a statistical point of view, and with a 10% of probability of being wrong when rejecting the null hypothesis, 33% and 36% are equal



- Independent samples
- Nominal and ordinal table
- Assumptions:
 - $N > 20$
 - $E \geq 5$ in at least 20% of cells (in 100%)

CV 87

χ^2

Exercise 3 A total of 210 emphysema patients entering a clinic over a 1-year period were treated with one of two drugs (either the standard drug, A, or an experimental compound, B) for a period of 1 week. After this period, each patient's condition was rated as greatly improved, improved, or no change. The sample results are shown below.

Therapy	Patient's Condition			
	No Change	Improved	Greatly Improved	
A	20 (16.67)	35 (38.09)	45 (45.24)	100
B	15 (18.33)	45 (41.9)	50 (49.76)	110
	35	80	95	210

Perform a chi-square test of independence. Use level of significance $\alpha = .05$.

$$\begin{aligned} \chi^2 = \sum \frac{(O - E)^2}{E} &= \frac{(20 - 16.67)^2}{16.67} + \frac{(35 - 38.09)^2}{38.09} + \frac{(45 - 45.24)^2}{45.24} + \frac{(15 - 18.33)^2}{18.33} + \frac{(45 - 41.9)^2}{41.9} + \\ &+ \frac{(50 - 49.76)^2}{49.76} = \frac{3.33^2}{16.67} + \frac{(-3.33)^2}{18.33} + \frac{(-3.09)^2}{38.09} + \\ &+ \frac{3.1^2}{41.9} + \frac{(-0.24)^2}{45.24} + \frac{0.24^2}{49.76} = \frac{11.09}{16.67} + \frac{11.09}{18.33} + \frac{9.55}{38.09} + \\ &+ \frac{9.61}{41.9} + \frac{0.06}{45.24} + \frac{0.06}{49.76} = 0.66 + 0.6 + 0.25 + 0.23 + 0.001 + 0.001 = \\ &= 1.742 \end{aligned}$$

$$df = (rows - 1) \times (columns - 1) = (2 - 1) \cdot (3 - 1) = 1 \cdot 2 = 2$$

$$\chi^2_{(0.05, 2)} = 5.99$$

χ^2 1.74 < χ^2_{α} 5.99 — H_0 There are not differences between treatments A and B (one drug is not better than the other with a 95% of level of confidence)

EXERCISE 4

$\hat{\rho} = 0.019 < 0.05$ — ~~H₀~~ ^(a) There is statistically significant relationship
(marked with asterisk)

(b) $r^2 = 0.37^2 = 0.14 < 0.18 \rightarrow$ Low effect size

NO, because the statistical significance can be due to an excessively high statistical power.

(c) $1 - CD = 1 - r^2 = 1 - 0.14 = 0.86$

86% of the variability of Y (height) is not explained by X (weight)