

PRACTICE 8

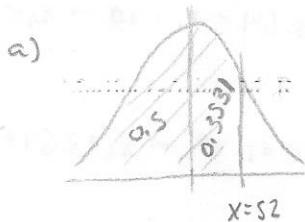
LESSON 5

33) The scores of a group of subjects is one variable following the normal law, with a mean of 40 and standard deviation of 8. With this data:

- Calculate the percentage of people who obtain a raw score equal to or less than 52.
- Calculate the percentage of people with scores between 24 and 48.
- Calculate the percentage of people with one score equal to or less than 30.
- Which score leaves below itself 60% of the cases?
- Which is the minimum score of 60% of subjects with higher scores?
- Calculate the two scores among which are the central 95% of the data.
- Which score delimit the 28% most extreme data?
- Which raw score leaves above itself 10% of the cases?
- Calculate the percentile 40.

$$\bar{x} = 40$$

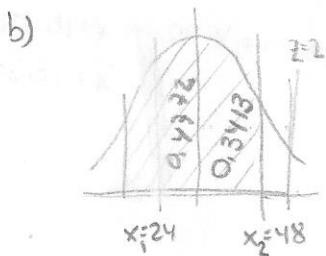
$$s = 8$$



$$z = \frac{X - \bar{X}}{s} = \frac{52 - 40}{8} = \frac{12}{8} = 1.5$$

$$p = 0.5 + 0.4332 = 0.9332$$

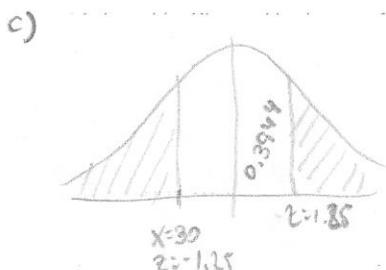
$$\% = 93.32$$



$$z_1 = \frac{X - \bar{X}}{s} = \frac{48 - 40}{8} = \frac{8}{8} = 1 \rightarrow p(z=1) = 0.3413$$

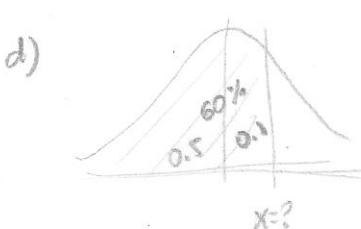
$$z_2 = \frac{X - \bar{X}}{s} = \frac{24 - 40}{8} = \frac{-16}{8} = -2 \rightarrow p(z=-2) = 0.4772$$

$$p(-2 \leq z \leq 1) = 0.3413 + 0.4772 = 0.8185 \rightarrow \% = 81.85$$



$$z = \frac{X - \bar{X}}{s} = \frac{30 - 40}{8} = -1.25$$

$$p(z \leq 30) = 0.5 - 0.3944 = 0.1056 \rightarrow \% = 10.56$$

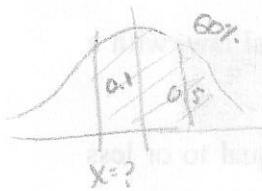


$$p = 0.6 \rightarrow z = 0.25$$

$$z = \frac{X - \bar{X}}{s} \rightarrow 0.25 = \frac{X - 40}{8} \rightarrow 8 \cdot 0.25 = X - 40 \rightarrow 2 = X - 40$$

$$42 = X$$

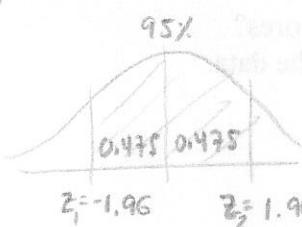
e)



$$z = -0.25$$

$$z = \frac{x - \bar{x}}{s} \rightarrow -0.25 = \frac{x - 40}{8} \rightarrow -2 = x - 40 \rightarrow x = -2 + 40 = 38$$

h)



$$z_1 = -1.96 \quad z_2 = 1.96$$

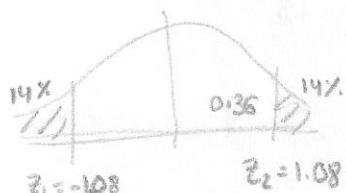
$$z = \frac{x - \bar{x}}{s} \rightarrow -1.96 = \frac{x_1 - 40}{8} \rightarrow -15.68 = x_1 - 40$$

$$\boxed{-15.68 + 40 = x_1 \\ 24.32 = x_1}$$

$$1.96 = \frac{x_2 - 40}{8} \rightarrow 15.68 = x_2 - 40$$

$$\boxed{15.68 + 40 = x_2 \\ 55.68 = x_2}$$

g)



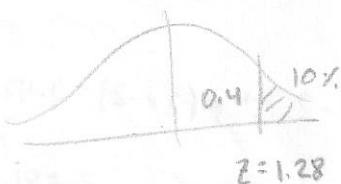
$$z_1 = -1.08$$

$$z_2 = 1.08$$

$$z = \frac{x - \bar{x}}{s} \rightarrow -1.08 = \frac{x_1 - 40}{8} \rightarrow -8.64 = x_1 - 40 \rightarrow x_1 = 8.64 + 40 = 31.36$$

$$1.08 = \frac{x_2 - 40}{8} \rightarrow 8.64 = x_2 - 40 \rightarrow x_2 = 8.64 + 40 = 48.64$$

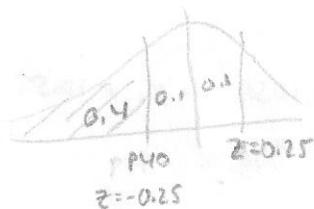
h)



$$z = 1.28$$

$$z = \frac{x - \bar{x}}{s} \rightarrow 1.28 = \frac{x - 40}{8} \rightarrow 10.24 = x - 40 \rightarrow x = 10.24 + 40 = 50.24$$

i) = e)



$$z = -0.25$$

$$z = \frac{x - \bar{x}}{s} \rightarrow -0.25 = \frac{x - 40}{8} \rightarrow -2 = x - 40 \rightarrow x = -2 + 40 = 38$$